# Teaching unit Multivariate calculus

## Course:

Mathematics 2 (8 ECTS credits, 1st year graduate students , 3 groups of 20-25 students), week 4

## Aim:

To foster mathematical and geometric intuition for understanding basic concepts of multivariate calculus (contour plot, partial derivatives, stationary points, extreme points, etc.)

## Activity 1: The revision of the basic terms (contour plot, partial derivatives)

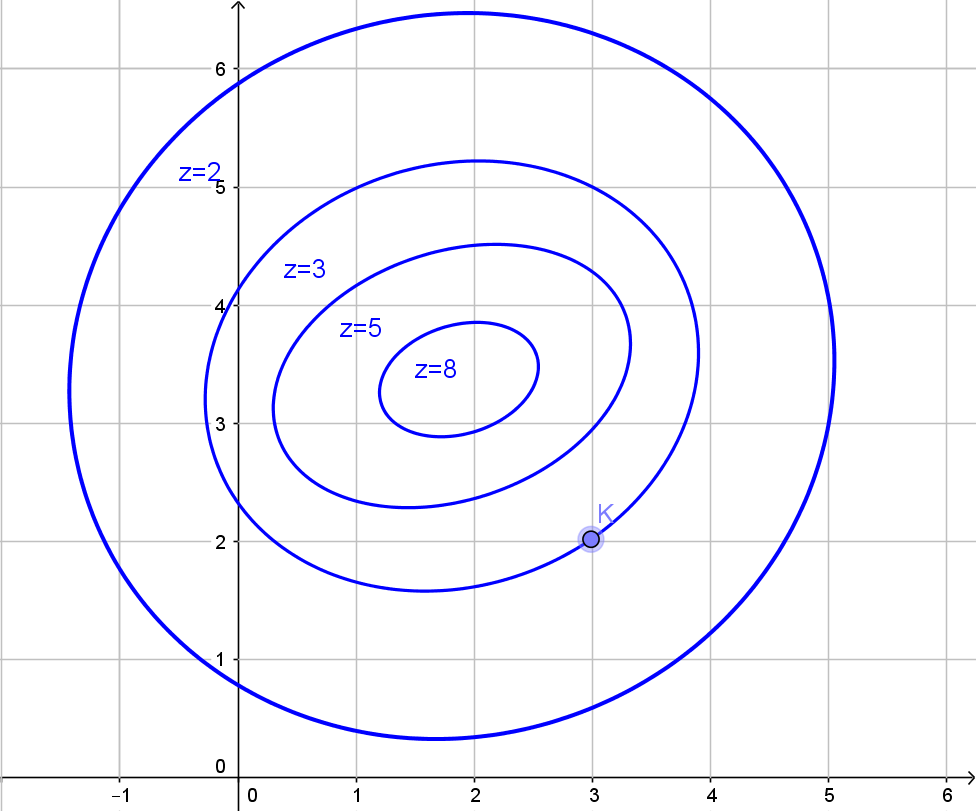
Answer the questions 1, 2 of the quiz on Classroom voting system Socrative (room BE483461)

### Problem 1:

The figure depicts the contours of the function z=f(x,y). Find the solution of the equation f(x,5)=3.

### Problem 2:

Suppose that the function z=f(x,y) has both partial derivatives in the point K=[3,2]. Try to determine their signs.

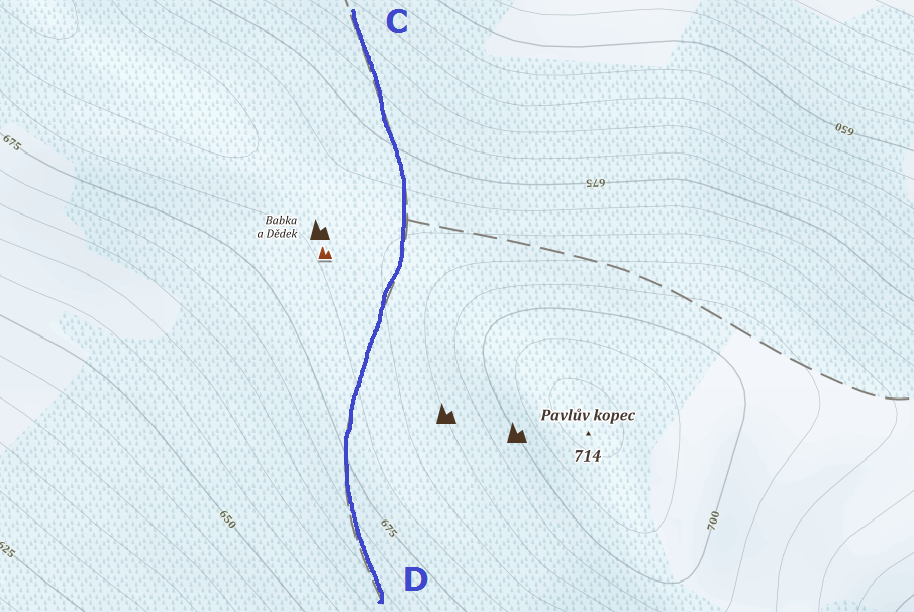


## Activity 2: Multivariate optimization

Solve the problems 1-3 in groups of three or four (1 handout for each group). Completing the tasks is followed by the discussion.

### Problem 1:

Find the lowest and the highest point on the path from C to D



### Problem 2:

Find the lowest and the highest point on the path from A to B



Supplementary questions:

- can you see any extrema points on the map?

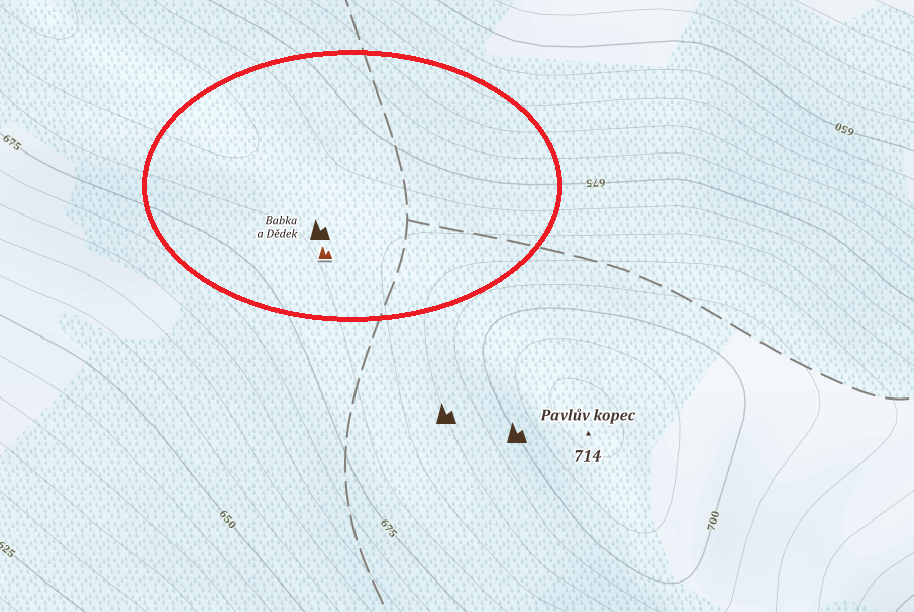
- describe the relation betweeen the density of contours and „the steepness of the surface“.

- why is the highest place on the path CD and the lowest place on AB represented by the same point?

- can you identify a saddle point on the map?

### Problem 3:

Find the lowest and the highest point in the selected region.



Supplementary questions:

- does the maximum lie inside the region or on the boundary?

- does the minimum lie inside the region or on the boundary?

- are both partial derivatives equal to zero in the extrema points?

- try to characterize the possible locations of extrema points .